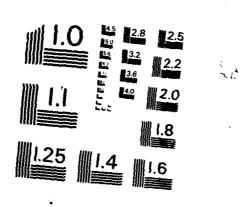
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SCATTERING COEFFICIENTS AND THE ABSORPTION EDGE OF LONGITUDINAL COHERENT SOUND WAVES IN SELECTED INHOMOGENEOUS MATERIALS

BY K. P. SCHARNHORST W. M. MADIGOSKY E. BALIZER

RESEARCH AND TECHNOLOGY DEPARTMENT

28 JUNE 1985



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The first three terms in the far field for	ward scattering amplitude for
longitudinal waves impinging on spherical object	s embedded in various matrix
materials were studied as functions of frequency	. The major resonances in
these terms were used to obtain rough estimates (of the position of the ab-
sorption edge in corresponding elastic and visco	elastic inhomogeneous material
It has been generally known that in relatively co	ompressible inhomogeneous
materials the lowest resonance frequency is that	
by means of highly compressible fluid inclusions	in soft rubbery media. Not

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20. Abstract (Cont.)

as widely known has been the fact that in incompressible materials the lowest achievable resonance frequency is that of the dipole. It occurs in relatively soft, rubbery media with heavy solid inclusions. By ordering our materials with respect to the lowest frequency at which significant scattering occurs, we put these observations into perspective. We also give an estimate of the absorption edge for every material combination in this study. A special effor is made to trace the development of the first three resonances in elastic solids as functions of the material properties of the host and the inclusion. We find that the monopole quickly moves to higher frequencies than the dipole as the compressibility of the inclusion is decreased, and that as a rule, these two terms interfere unless the mass density of the inclusion is much greater than that of the host.

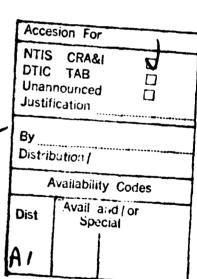
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CHAPTER 1

INTRODUCTION

In this study we examine the imaginary parts of the first three terms in the far field forward scattering amplitude for longitudinal plane waves impinging on spherical scatterers. A wide variety of different matrix materials is considered. The objective was to obtain an idea of the approximate location of the absorption edge of coherent sound waves due to resonant scattering from inclusions in inhomogeneous materials containing randomly distributed spherical scatterers at any concentration.

Evidently it would be best to calculate absorption directly. However, at all but the lowest concentrations of inclusions that would be a formidable task. On the other hand, if the basic resonances of the inclusions which show up in the imaginary part of the scattering amplitude, f(0), are known, the approximate location of the absorption edge may be inferred. It is clear on physical grounds that the lowest frequencies at which this edge can possibly occur are those at which resonant scattering of the individual inclusions sets in. In any given situation, measurable absorption may occur at somewhat higher frequencies in an inhomogeneous material, but it certainly cannot occur at significantly lower ones. If there is a shift to lower frequencies, it should be due to volume concentration effects; due to the number of single and multiple scattering events per unit volume. As these events multiply with the concentration of inclusions, the effects of individual resonances add and increase absorption. Of course, scattering in directions other than forward and backward should also be considered. But the resonance frequencies do not depend on angular variables; hence, the scattering coefficients in f(0) contain all the information we need to locate the absorption edge. The forward scattering amplitude provides a convenient conceptual framework.

In this sense we are studying the absorption edge independently of any particular theory. The edge is of great interest to the materials designer whose task it may be to push it to the lowest frequency he can possibly reach within given material constraints.

As an example illustrating how the coefficients of the longitudinal scattering amplitude might enter into an expression for the absorption length, we quote the results of the Waterman-Truell theory 1 in the following section. In certain limiting situations their expression for the longitudinal effective wave vector yields the classical first order result. 2

CHAPTER 2

SCATTERING COEFFICIENTS AND ABSORPTION IN INHOMOGENEOUS MATERIALS; AN EXAMPLE

The Waterman-Truell theory of propagation of coherent longitudinal sound waves in inhomogeneous materials with randomly distributed scatterers yields the following rather simple looking expression for the effective wave vector:

$$K_{eff} = \frac{\omega}{C_{eff}} + i\alpha_{eff} = K \left\{ 1 + \left(\frac{3\phi}{K^2 A^3} \right) f(0) + \frac{1}{4} \left(\frac{3\phi}{K^3 A^3} \right)^2 (f^2(0) - f^2(\pi)) \right\}^{1/2}$$
 (1)

where K = K(Cd₁) is the wave vector of the matrix material, A the radius of the inclusion, ϕ the volume fraction of the inclusions and f(0) and f(π) are the plane wave forward and back scattering amplitudes respectively, as calculated from the scalar potential function of the problem. Ceff is the effective wave speed and $1/\alpha_{\rm eff}$ the effective absorption length.

At low concentrations of inclusions, or whenever $[f^2(0) - f^2(\pi)] << 1$, the quadratic term may be neglected, the square root expanded to first order and one obtains:

$$\alpha_{\text{eff}} = \text{Im}(\mathbf{K}_{\text{eff}}) \simeq \text{Im}\left[\mathbf{K}\left\{1 + \frac{1}{2}\left(\frac{3\phi}{\mathbf{K}^2\mathbf{A}^3}\right) f(0)\right\}\right]$$
 (2)

This is the classical first order result.2

In terms of the coefficients of the longitudinal scattering potential one finds that:

$$f(0) = \frac{1}{iK} \sum_{n=0}^{\infty} i^{-n} a_n = f_e(0) + f_o(0)$$
 (3)

and:

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$$t(\pi) = \frac{1}{iK} \sum_{n=0}^{\infty} (-i)^{-n} a_n = f_e(0) - f_o(0)$$
 (4)

where $f_e(0)$ and $f_o(0)$ are sums over even and odd n in f(0) respectively. Substituting into Eq. 1, one finds:

$$K_{\text{eff}} = K \left\{ 1 + \left(\frac{3\phi}{K^2 A^3} \right) f(0) + \left(\frac{3\phi}{K^2 A^3} \right)^2 f_{\text{e}}(0) f_{\text{o}}(0) \right\}^{-1/2}$$
 (5)

or:

$$K_{eff} = K \left\{ 1 + (-X_0 - X_1 + X_2 \pm ...) + (X_0 X_1 - X_1 X_2 \pm ...) \right\}^{-1/2}$$
 (6)

up to n = 2, where:

$$X_{0} = \frac{3i\phi a_{0}}{(KA)^{3}}$$

$$X_{1} = \frac{3\phi a_{1}}{(KA)^{3}}$$

$$X_{2} = \frac{3i\phi a_{2}}{(KA)^{3}}$$
(7)

The imaginary parts of these expressions are the three functions studied in this paper.

Evidently, in elastic host materials the inverse absorption length in Eq. 1, $\alpha_{\rm eff}$, is simply related to the imaginary parts of quantities like X_i and X_j X_k in Eq. 6, where j = even and k = odd. When these are small, attenuation of coherent waves approaches zero. When they are large, or more accurately when the appropriate sums of the imaginary parts in the brackets in Eq. 6 become significantly different from zero, absorption becomes important. By studying these coefficients we therefore obtain a first impression as to where to expect the absorption edge in various combinations of matrix materials and inclusions.

We focus on the first three coefficients, the monopole (n = 0), the dipole (n = 1), and the quadrupole (n = 2). We find that in most cases either the monopole or the dipole yields the lowest resonance frequency. Often the quadrupole is near one or the other of these. Assuming that still higher order resonances are weak or occur well above the first three, the approximate frequency region of the absorption edge may be read directly off our plots of $Im(X_1)$, i = 0,1,2.

We have plotted only $\operatorname{Im}(X_1)$, which is all we need to do in order to understand the lowest order theory, Eq. 2. In the case of the Waterman-Truell theory we could have obtained a more complete picture of α_{eff} , if we had also plotted $\operatorname{Re}(X_1)$, since the cross-terms, $\operatorname{Im}(X_j|X_k)$, use both of these components. But clearly, for our purpose, which is to detect the lowest frequency at which the edge could possibly occur in any theory, the study of $\operatorname{Im}(X_1)$, which contains the typical resonance peaks is entirely sufficient.

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CHAPTER 3

GENERAL REMARKS

We have collected the data in several groups of related material characteristics; Tables 1 and 2. Listed are the first Lamé parameter, $\lambda^* = \lambda \; (1-i\eta_\lambda)$, the shear modulus, $\mu^* = \mu \; (1-i\eta_\mu)$ and the mass density, ρ , of the host (1) and the inclusion (2). Both λ and μ have been reduced by the modulus of water. Some of the materials in these groups are on the verge of being unrealistic, such as porous metallic inclusions and certain materials with rather high relaxation absorption. These have been included in order to study the outer limits of material parameter combinations.

The moduli were assumed to be independent of frequency. This is a potential problem if the size of the resonator is assumed to be such that the resonances appear in the relaxation region of the shear modulus. The present work might be extended in that direction.

The parameters of foamed rubber were generated with the aid of the Kerner (quasi-static) theory, 3 using reasonable rubber parameters as input and 40% air. Here we assume that the individual air pockets in the resulting foam are small, hence far from the resonances of the inclusions.

We have plotted the imaginary parts of $-X_0$, $-X_1$, and X_2 in all of our figures, since X_0 and X_1 are negative. Also, many of the minor resonances contain scaling factors. The dominant resonance is approximately full scale. A scaling factor of -5 for instance means that $Im(X_1)$ has been multiplied by -5. This would be indicated in the figure caption as $X_1(-5)$. The reader is cautioned to check these numbers before judging the relative strengths of the resonances.

All of our data is plotted versus the real part of $K(C_{d_1})xA$ of the matrix material, which is obtained when the loss tangents of λ_1^* and μ_1^* are equated to zero. Note that the result is not the same as Real $(K(C_{d_1})xA)$. But it allows the reader to compare otherwise similar elastic and viscoelastic materials directly. At the left hand end of the abscissa we also indicate the corresponding frequency, assuming 2mm for the radius, A, of the inclusion, thus enabling the reader to shift the data on the frequency axis when the radius is changed.

The frequency in the leading edge of the lowest frequency major resonance in each figure, f_{Γ} , at which Im(X) reaches one half its maximum, is a measure of the frequencies at which reasonably strong absorption might be expected in each

TABLE 1. MATERIAL PARAMETERS OF ELASTIC MATERIALS; FIGURES 1-6 AND 9-21

The second second

		MATERIAL		Ŗ	¥	Ż	ķ	ŧ	ķ		Metallic Material	Gless	Porous Metai	Heavy Silicone Rubber	Steel		Metallic Material	Porous Metal	Steel	Stool	Heavy Silicone Rubber		Heavy Silicone Rubber	Heavy Silicone Rubber	Herry, Loaded Silicone Pubber
		83	li .	0.00121	0.00121	0.00121	0.00121	0.00121	0.00121		2.0	2.49	0.249	70	7.84		2.49	0.40	7.84	7.84	1.71		20	20	7
	NOIS	742		ö	ö	ö	ö	ö	Ģ		ö	Ö	ð	ö	ď		ë	ö	ö	ë	ö		ö	ಪ	ð
	INCLUSION	Н		c i	Ü	ď	ď	ej	ď	TRICES	11.6	11.6	11.6	1.422×10^{-3}	33.486		10.0	10.0	33.486	33.486	4.028×10^{-3}		1.422×10^{-4}	1.422×10^{-3}	1,422 × 10 ⁻³
		71,2	SO	ei	ď	6	ö	6	ö	BER MA	ö	6	ö	ø	ö	83	ö	Ö	ö	Ö	ö	¥!	Ö	Ö	c i
ELASTIC MATERIALS		γ	AIR FILLED CAVITIES IN ELASTIC SOLIDS	6.31×10^{-5}	6.31×10^{-5}	6.31×10^{-5}	6.31×10^{-5}	6.31×10^{-5}	6.31×10^{-5}	ELASTIC MATERIALS IN PLASTIC AND HARD RUBBER MATRICES	40.09	8.05	40.09	0.604	55.97	ELASTIC MATERIALS IN RUBBER MATRICES	43.29	43.29	55.97	55.97	0.527	ELASTIC MATERIALS IN SYNTACTIC FOAM	0.606	0.604	0.150
ELASTI		MATERIAL	AIR FILLED CAVIT	Rubber	Hard Rubber	Foamed Rubber	Plastic	Syntactic Foam	Steel	MATERIALS IN PLAS	Plastic	Plastic	Plastic	Hard Rubber	Plastic	ELASTIC MATERIAL	Rubber	Rubber	Rubber	Vory Soft Rubber	Sificone Rubber	ELASTIC MATERIA	Syntactic Foam	Syntactic Foam	Syntactic Foam
	- 1	6		1.13	1.19	0.50	1.18	0.689	7.84	ELASTIC	1.18	1.18	1.18	==	1.18		1.13	1.13	1.18	1.18	1.02		0.689	0.689	0.689
	ATERIA	ואנ		ö	-		6	=	0		6	ë	.		.		6	ö	6	.	=		ö	ö	5
	MATRIX MATERIAL	н		0.0044	90.0	0.0017	0.70	0.689	33.486		0.70	0.70	0.70	9920:0	0.70		0.0044	0.0044	0.0044	4.4 × 10 ⁻⁵	3.45 × 10 ⁻⁴		689	989	689 .
		א או		ø	c i	ö	ö	Ö	ö		-	æ	c i	6	Ö		0	ö	o	-	Ö		=	ö	.
		,		0.975	1.25	0.0048	2.048	0.854	55.97		2.048	2.048	2.048	1.545	2.048		0.975	0.975	0.972	0.972	0.531		0.854	0.854	0.854
		.		-	7	ო	~	ĸ	40		en en	2	=	12	5		=	15	16	11	8 2		61	R	23

TABLE 2. MATERIAL PARAMETERS OF VISCOELASTIC MATERIALS; FIGURES 22-33

VISCOELASTIC MATERIALS

	MATERIAL		Heavy Silicone Rubber	Heavy, Loaded Silicone Rubber	Heavy, Loaded Silicone Rubber	Heavy, Loaded Rubber	Heavy Sificone Rubber		Plastic	Heavy, Loaded Plastic	Heavy Silicone Rubber		Heavy Silicone Rubber	Heavy Sificone Rubber	Heavy Loaded Sificone Rubber	Heavy Loaded Plastic
	w		2.0	9;	4.6	6.	2.0		0 :	0.4	1.71		2.0	2.0	6.0	9;
INCLUSION	24/7		0.16	0.16	0.16	0.16	0.16		9.5	0.5	88		0.16	0.16	0.16	0.50
<u>S</u>	H2	MATRICES	1.422×10^{-3}	2.84 × 10 ⁻⁴	2.84 × 10 ⁻³	2.84×10^{-3}	1.422×10^{-3}	BBER MATRICES	0.44	0.444	4.028 × 10 ⁻³		1.422 × 10 ⁻³	1.422×10^{-4}	1.422 × 10 ⁻³	0.44
	71/2	RUBBER	6	c i	ó	6	Ö	VMED RU	ð	Ġ	ö	C FOAM	e i	Ö	5	9
	24	STIC AND HARD	0.604	0.159	0.154	1.208	10.604	RUBBER AND FOA	1.334	1.334	0.527	ALS IN SYNTACTI	0.694	0.606	0.150	1.334
	MATERIAL	VISCOELASTIC MATERIALS IN PLASTIC AND HARD RUBBER MATRICES	Hard Rubber	Heavy Plastic	Heavy Plastic	Heavy Plastic	Plastic	VISCOELASTIC MATERIALS IN SILICONE RUBBER AND FOAMED RUBBER MATRICES	Silicone Rubber	Silicone Rubber	Silicone Rubber	VISCOELASTIC MATERIALS IN SYNTACTIC FOAM	Syntactic Foam	Syntactic Foam	Syntactic Foam	Syntactic Foam
_11	2	COELASTIC	1.1	1.985	1.985	1.985	1.213	STIC MAT	1.0	0.1	1.02	Š	0.689	0.689	0.689	0.689
MATERIA	n n n	VISC	0.45	0.0098	0.0109	0.0109	0.01	ISCOELAS	1.0	0.1	0.12		0.01	0.01	0.01	0.01
MATRIX MATERIAL	z		2.655 × 10 ⁻²	0.282	0.282	0.282	0.2094	> 1	4,44 × 10 ⁻³	4.44 × 10 ⁻³	3.45 × 10 ⁻⁴		.689	.689	689	.689
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	7		1.545	0.4228	0.4186	1.028	0.824		0.44	0.444	0.531		0.854	0.854	0.854	0.854
	E *		u	23	24	22	æ		n	82	Ø		8	31	33	æ

system. Note that this frequency is independent of the assumed volume fraction of inclusions. f_{Γ} is given in each figure caption and all of these frequencies are summarized in Table 3.

We have also done a more systematic study of the displacements of the first three multipoles with changes in the material parameters. The results are collected in Table 4 and Fig. 8. Again some unrealistic materials are included, this time in order to achieve a continuous sequence of parameter combinations. Only elastic materials were considered. Some of these are also included in Table 1. Again we have studied $Im(X_1)$ rather than a_1 . The frequencies of the major resonance peaks in each of these materials are displayed in Fig. 8. Some idea of the widths of the peaks may be obtained by referring to the explicit plots of the resonances in elastic material combinations which are common to both parts of this study.

Because of the inclusion of viscoelastic materials in this study it might have been more appropriate to consider $i^{-(n+1)} a_n/K^2$ rather than $i^{-(n+1)} a_n/K^3$ in order to estimate the position of the absorption edge, since the factor K in front of the curly bracket in Eq. 2 mixes the real and imaginary parts of the terms inside whenever viscoelastic materials are considered. We have checked this effect in the case of example #27 in Table 2; i.e., for a plastic in silicone rubber. f_{Γ} increased by 10% and the quadrupole (main) resonance frequency increased by 15%.

Calculations were performed in two ways: On the basis of the classical solutions of these problems as given by Yamakawa $(1962)^4$ as well as on the basis of the T-matrix solution given by Waterman $(1976)^5$ and Pao (1978).6 These are two completely independent approaches to these problems. Our numerical calculations give identical results. Numerical difficulties with the classical solution, due to extremely large and extremely small elements in the same matrix (2x2 when n=0, 4x4 when n>0) were overcome in the frequency intervals treated here, by appropriately scaling the columns and/or the rows. Such problems occurred only occasionally and then only at the highest or the lowest frequencies, never in the resonance region itself. With the T-matrix method, no computational problems at all were encountered.

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Whenever asymptotic formulas were applicable, such as in the case of air cavities in rubber and heavy inclusions in rubbery matrices, the results so obtained agreed very well with our numerical calculations.

The concentration of inclusion, ϕ , in Eq. 7 was arbitrarily assumed to be 1%.

TABLE 3. EDGE FREQUENCIES, \mathbf{f}_{Γ} , OF VARIOUS MATERIAL COMBINATIONS

#	FIG. #	f (kHz)	HOST MATERIAL	INCLUSION
1	17	0.44	Very Soft Rubber	Steel
2	29	2.20	Silicone Rubber	Heavy Silicone Rubber
3	18	2.30	Silicone Rubber	Heavy Silicone Rubber
4	16	4.20	Rubber	Steel
5	28	5.60	Silicone Rubber	Heavy Loaded Plastic
6	14	6.70	Rubber	Metal
7	3	9.6	Foamed Rubber	Air
8	15	12.8	Rubber	Porous Metal
9	1	13.0	Rubber	Air
10	24	33.4	Heavy Plastic	Heavy, Loaded Silicone Rubber
11	23	34.2	Heavy Plastic	Heavy, Loaded Silicone Rubber
12	32	39.6	Syntactic Foam	Heavy, Loaded Silicone Rubber
13	21	40.2	Syntactic Foam	Heavy, Loaded Silicone Rubber
14	2	42.2	Hard Rubber	Air
15	25	42.6	Heavy Plastic	Heavy, Loaded Rubber
16	26	51.5	Plastic	Heavy Silicone Rubber
17	13	56.2	Plastic	Steel
18	33	67.9	Syntactic Foam	Heavy, Loaded Plastic
19	30	81.7	Syntactic Foam	Heavy Silicone Rubber
20	31	81.7	Syntactic Foam	Heavy Silicone Rubber
21	20	82.8	Syntactic Foam	Heavy Silicone Rubber
22	10	83.6	Plastic	Glass
23	19	85.6	Syntactic Foam	Heavy Silicone Rubber
24	27	96.6	Silicone Rubber	Plastic
25	22	113.0	Hard Rubber	Heavy Silicone Rubber
26	12	116.8	Hard Rubber	Heavy Silicone Rubber
27	4	125.9	Plastic	Air
28	11	141.3	Plastic	Porous Metal
29	5	149.6	Syntactic Foam	Air
30	9	168.2	Plastic	Metal
31	6	316.2	Steel	Air

TABLE 4. MATERIAL PARAMETERS OF ELASTIC MATERIALS; FIGURE 8

	MATRIX	MATERIAL				INCLUSION	
#	λ ₁	μ1	Q1		λ2	μ2	Q2
1	55.97	33.49	7.84		6.33 × 10 ⁻⁵	0	0.00121
2	2.048	0.7	1.18		6.33 × 10 ⁻⁵	0.	0.00121
3	0.972	0.0044	1.13		6.33 × 10 ⁻⁵	0.	0.00121
4	0.972	0.0044	1.13	1	6.33 × 10 ⁻³	0.	0.00121
5	0.972	0.0044	1.13		5.33 × 10 ⁻²	0.	0.00121
6	0.972	0.0044	1.13		6.33 × 10 ⁻²	10 ⁻⁶	0.00121
7	0.972	0.0044	1.13		63.3	10-6	0.00121
8	0.972	0.0044	1.13		63.3	10-4	0.00121
9	0.972	0.0044	1.13		63.3	10-2	0.00121
10	0.972	0.0044	1.13		62.3	0.5	0.00121
11	0.972	0.0044	1.13		43.3	10.0	0.00121
12	0.972	0.0044	1.13		43.3	10.0	0.12
13	0.972	0.0044	1.13		43.3	16.0	0.30
14	0.972	0.0044	1.13		43.3	10.0	0.40
15	0.972	0.0044	1.13		43.3	10.0	0.50
16	0.972	0.0044	1.13		43.3	10.0	1.00
17	0.972	0.0044	1.13		43.3	10.0	1.75
18	0.972	0.0044	1.13		43.3	10.0	2.49
19	3.44	0.0044	1.13		43.3	10.0	0.12
20	3.31	0.07	1.18	·	43.3	10.0	0.12
21	2.048	0.7	1.18	į	43.3	10.0	0.12
22	2.048	0.7	1.18		40.09	11.6	0.12
23	2.048	0.7	1.18		40.09	11.6	0.12
24	2.048	0.7	1.18		40.09	11.6	0.249
25	2.048	0.7	1.18		40.09	11.6	1.00
26	2.048	0.7	1.18		40.09	11.5	1.50
27	2.048	0.7	1.18		40.09	11.6	2.00
28	2.048	0.7	1.18		40.09	11.6	2.49
29	2.048	0.7	1.18		8.05	11.6	0.249
30	3.43	0.0077	1.18		8.05	11.6	0.249
31	3.43	0.0077	1.18		8.05	11.6	2.49
32	2.048	0.70	1.18		8.05	11.6	2.49
33	2.048	0.7	0.50		8.05	11.6	2.49
34	2.048	0.7	1.18		55.97	33.49	7.84

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CHAPTER 4

RESULTS AND DISCUSSION

ELASTIC MATERIALS

Air Filled Cavities in Elastic Solids

The most conspicuous feature here is that the monopole always occurs at a lower frequency than the dipole. However, usually the two resonances overlap and the quadrupole also mixes in. But in one case, that of an air cavity in rubber, Figs. 1 and 2, the monopole is the only important resonance. In that case, $K(C_{d_1})xA$ is small and the resonance frequency, f_0 , as well as the amplitude, $f_0(f_0)$ and the width $f_0(f_0)$ of the resonance in $f_0(f_0)$ may be calculated from the resonance of the first term in Eq. 3.7,8 Substituting into Eq. 7, we find:

$$f_o = \frac{C_{s_1}}{\pi A} \text{ or } K(C_{d_1}) A = \frac{1}{\alpha}; \alpha = C_{d_1}/2 C_{s_1}$$
 (8)

$$X_0(f_0) = -3\phi\alpha^3 \tag{9}$$

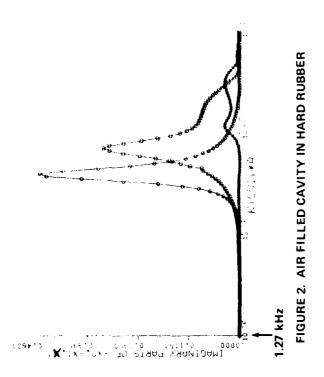
$$\Gamma = 1/\alpha^2 \tag{10}$$

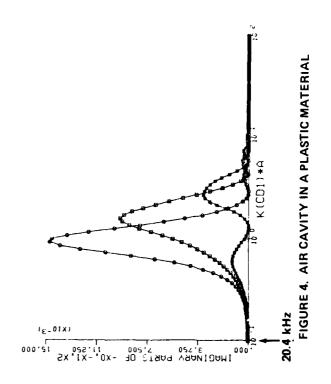
Note how much larger and narrower this resonance is compared to all of the others in this group.

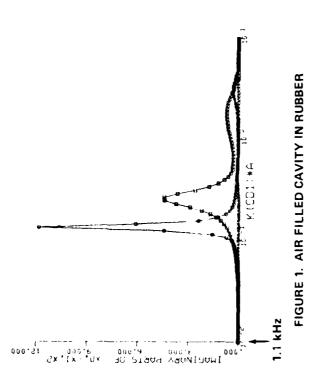
In the other examples, Figs. 3-6, Eqs. 8-10 should no longer apply, since $K(C_{d_1})xA$ is no longer small. However, we find that Eq. 8 still yields the resonance frequency with reasonable accuracy. In Fig. 7 we have plotted the halfwidths of the major resonance peaks in Figs. 1-6 versus the resonance frequency. Note that at large values of $K(C_{d_1})xA$ where Eq. 8 no longer applies, the halfwidths seem to depend approximately linearly on the resonance frequencies. When Eq. 8 applies, the relationship between f_O and Γ follows from Eqs. 8 and 10:

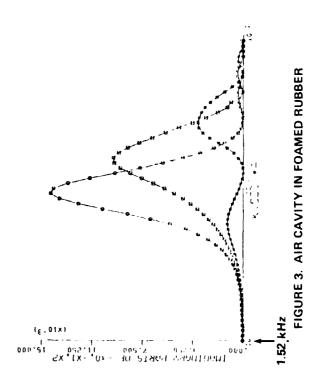
$$f_{o} = \frac{C_{d_1}}{2\pi A} \Gamma^{1/2}$$

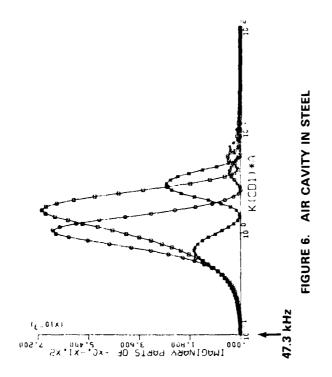
Hence in materials with giant monopoles and equal longitudinal wave speeds, the halfwidth of the monopole resonance depends quadratically on f_0 .

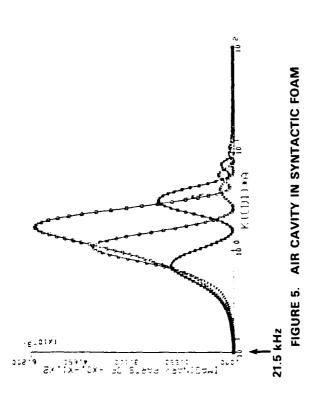












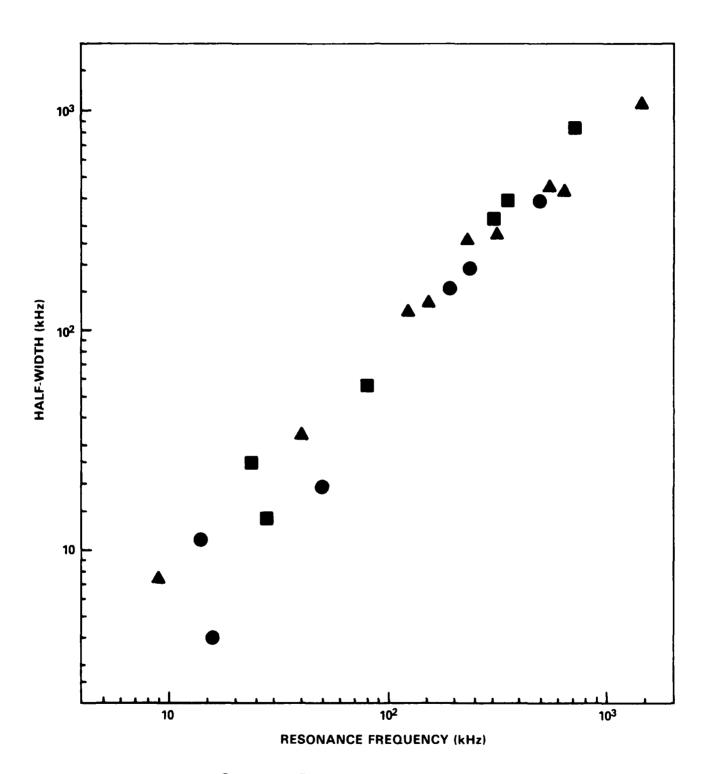


FIGURE 7. MONOPOLE (●), DIPOLE (■) AND QUADRUPOLE (▲) HALF WIDTHS AND RESONANCE FREQUENCIES OF AIR CAVITIES ON VARIOUS MATERIALS; TABLE 1 AND FIGURES 1-6

It has been argued in the past⁹ that a cavity in steel does not resonate in the monopole mode (or, more accurately, that the monopole resonance frequency is imaginary), essentially because the condition $(2C_{s_1}/C_{d_1})>1$, which is satisfied in that case, removes the resonance from the denominator of a_0 . Referring to Fig. 6 we would like to draw particular attention to the fact that not only does this resonance exist, but it is in fact rather prominent.

On the basis of our more systematic studies of elastic materials, Table 4 and Fig. 8, we may also make the following general statement about the first two multipoles in hard and soft rubber materials: Starting from an air filled cavity, as the compressibility of the inclusion material is decreased, the monopole moves to higher frequencies and has a strong tendency to pass the dipole (see the sequences 3 to 18 and 2, 21 to 29 in Table 4 and Fig. 8).

Elastic Materials in Plastic and Hard Rubber Matrices

The quadrupole tends to be a strong resonance in some of these examples and the dipole tends to occur at lower frequencies than the monopole. The latter is in fact the rule for solid inclusions in solids, as will become clear from the remainder of this study.

In the case of steel in plastic the dipole is the only significant resonance. It may be shown that in this case the resonance frequency of a_1 may be calculated from: 10

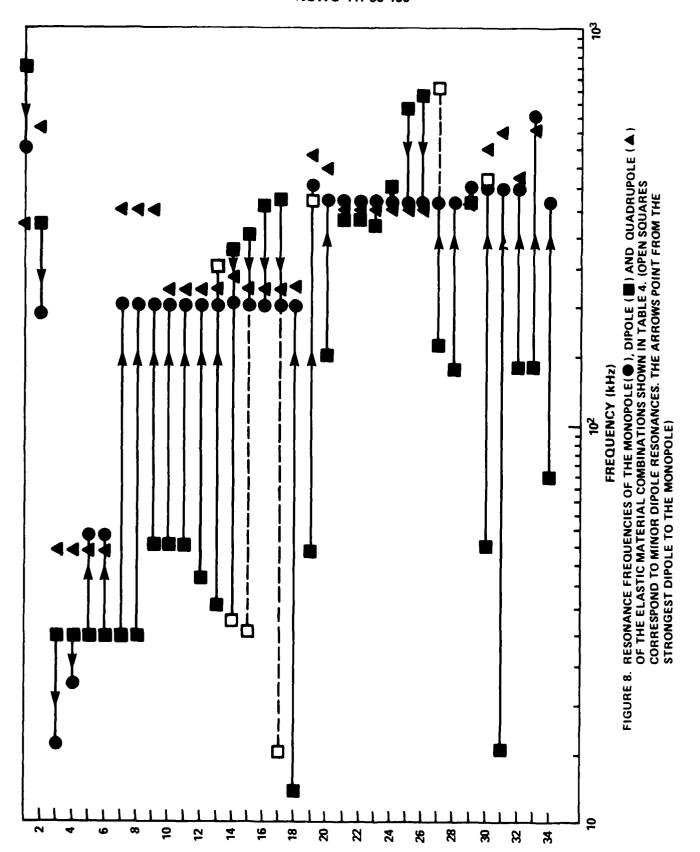
$$f_{o} = \frac{3C_{s_{1}}}{2\pi A} \sqrt{\frac{\rho_{1}}{2\rho_{2} + \rho_{1}}}$$
 (11)

or

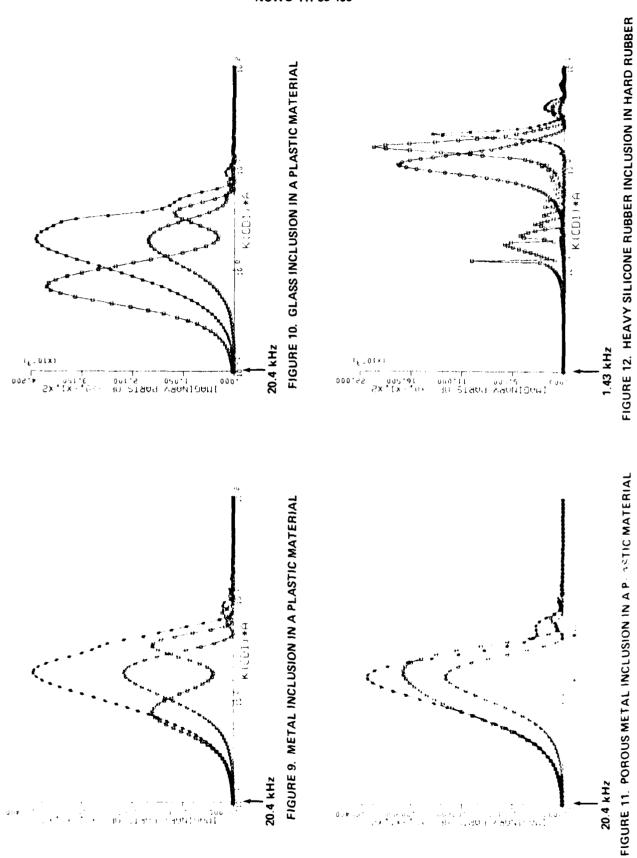
$$K(C_{d_1}) * A = 3 \sqrt{\frac{\mu_1 \rho_1}{(\lambda_1 + 2\mu_1)(2\rho_2 + \rho_1)}}$$
 (12)

The narrower this resonance, the more accurately Eq. 11 yields the resonance frequency of X_{l} .

We would also like to point out that the example in Fig. 10 has recently been used to illustrate a theory of the dynamic properties of inhomogeneous materials with tenuous random distributions of spherical inclusions. It was assumed quite generally that the monopole is the lowest resonance in solids with solid inclusions, which is clearly not the case in this particular example. Even if the monopole happens to be the lowest resonance, we have never observed it to be well separated from the dipole. An example of that type of situation is that of heavy silicone rubber in hard rubber, Fig. 12.



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Note that the host materials in Figs. 4, 9 and 13 are identical.

Elastic Materials in Rubber Matrices

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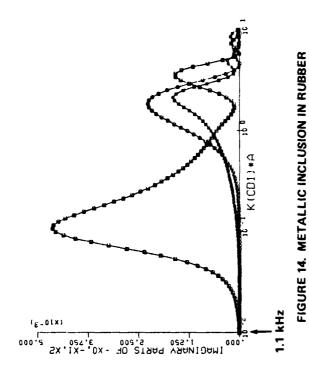
The dipole is clearly the lowest resonance in this group. It virtually dominates the spectrum at low frequencies. It can be moved to lower frequencies by increasing the mass of the inclusion and/or by decreasing the shear modulus of the host. The dipole resonance in Fig. 17 for instance (the lowest resonance observed in this study) is at $K(C_{d_1})*A = 5.34 \times 10^{-3}$ or $f_0 = 580$ Hz. In all examples, except that for porous metallic inclusions in rubber, it is possible to calculate the resonance frequency of the dipoles from Eq. 11.

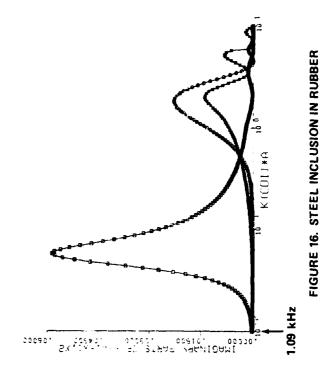
Note that the host materials in Figs. 1, 14, 15, and 16 are essentially the same.

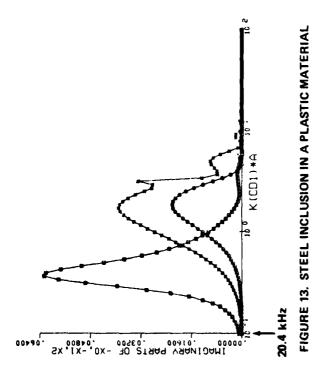
Also note that in going from Fig. 14 to Fig. 15, we are merely decreasing the mass of the inclusion. In Fig. 15 we observe a dipole double resonance. In going to Fig. 14, the low frequency peak of this resonance increases at the expense of the high frequency one. Had we decreased the mass, the high frequency peak would have increased at the expense of the low frequency one. We have observed this effect several times in other material combinations (see Table 4 and Fig. 8, sequences 11 to 18 and 23 to 29). Hence the motion of the dipole is not an outright motion of a single resonance, but rather an exchange of emphasis on two distinct resonance frequencies. But, as mentioned before, although the low frequency dipole resonance (heavy inclusion) may occur well below the monopole, the high frequency one (light weight inclusion), although above the monopole in frequency, remains close to it.

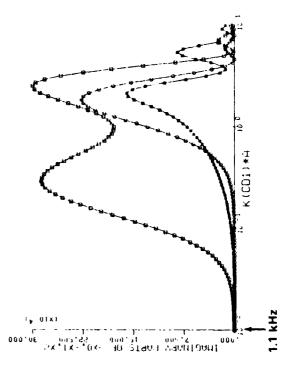
Combining these observations with our remarks on air filled cavities in elastic solids and drawing on our more detailed studies, Table 4 and Fig. 8, we may make the following general statement about the movements of the first two multipoles in rubber and plastic matrix materials: Starting with a light weight, highly compressible, low shear inclusion (air) in an elastic solid, the monopole is below the dipole. As we decrease the compressibility of the inclusion, regardless of its shear rigidity, while keeping its mass constant, the monopole resonance has a tendency to move to higher frequencies than the dipole. Here we are of course leaving the domain of real substances at ordinary temperatures (extremely lightweight but fairly incompressible). In order to return to real substance, we now increase the mass of the inclusion. To be specific, let us also assume that we have increased its shear rigidity. Hence we are dealing with a solid inclusion. The dipole first moves through the effect described above, until its major resonance occurs above that of the monopole, although close to it (entries 12 to 16 in Table 4 and Fig. 8). If we now keep increasing the mass of the inclusion, the same effect will bring the dipole back down below the monopole (see entries 16 to 18 in Table 4 and Fig. 8).

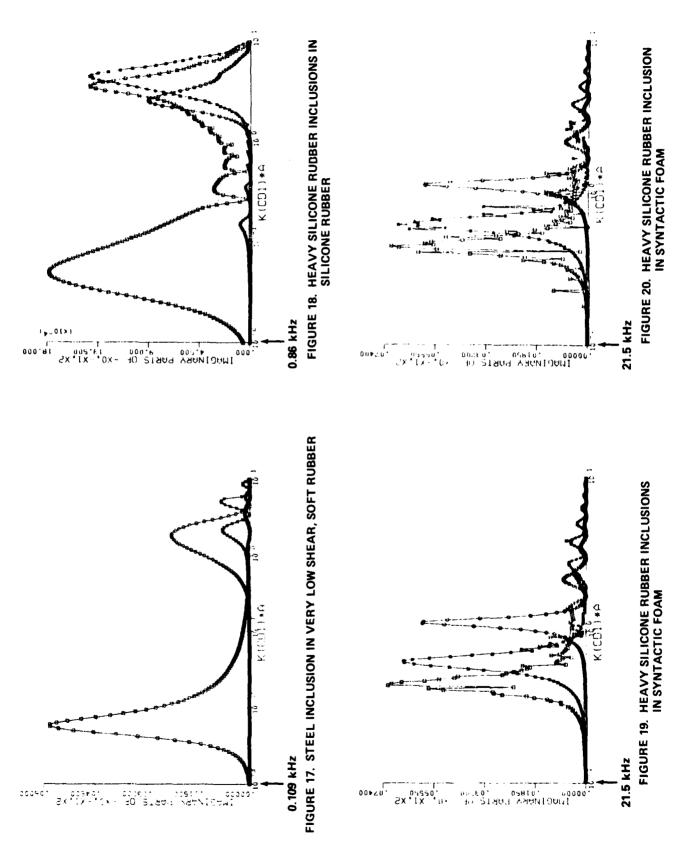
So far the host material has remained unchanged. As mentioned before, decreasing the shear rigidity of the host while increasing the mass of the











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inclusion will yield the lowest possible dipole frequencies. More generally, as a rule, the more waterlike the host medium, i.e., the smaller ${\rm C_{81}/C_{d1}}$, the lower the resonance frequencies of the dipole and the monopole. The general domains of the resonance frequencies of the two primary matrix materials in Table 4 and Fig. 8 illustrate this point. The matrix materials of examples 3 to 18, as well as of 30 and 31 are waterlike; those of examples 21 to 29, 32 to 34 as well as those of 1 and 2 are not. Examples 19 and 20 form a bridge between these sequences.

Elastic Materials in Syntactic Foam

Heavy elastic silicone rubber materials in elastic syntactic foams have a tendency to yield spectra in which the principal resonances are broken up into many minor ones. Our best example of this effect is shown in Fig. 21. If absorption is introduced, particularly into the rubber inclusions, yielding more realistic materials, the resonances become smooth again (see below).

Note that the host material in Fig. 5 is the same as the host material of the present group.

VISCOELASTIC MATERIALS

Viscoelastic Materials in Plastics and Hard Rubber Matrices

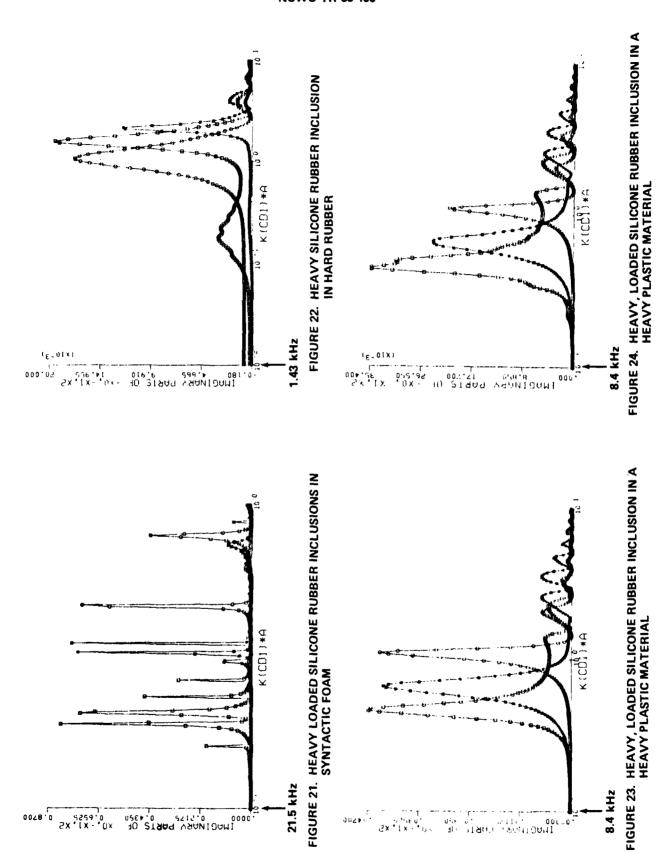
As before, the dipole is below the monopole in these solid-solid combinations, or if not, at least it overlaps it considerably. The latter is true for the example shown in Fig. 22, which is the example of Fig. 12, except that absorption was added.

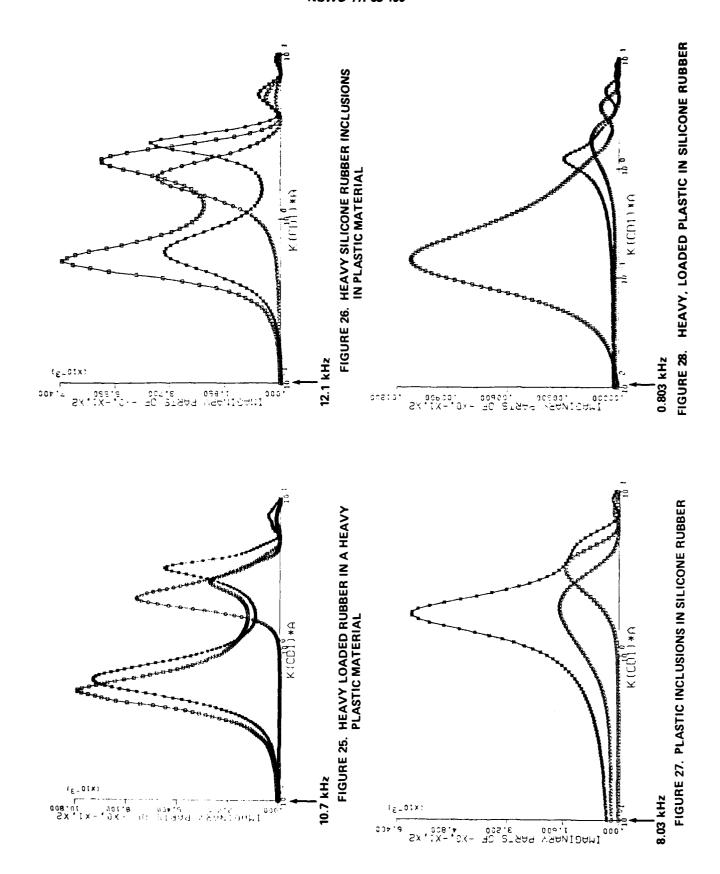
At low frequencies in Fig. 22 the dipole and quadrupole coefficients are negative. This does not mean of course that we are dealing with "negative absorption." Absorption must be calculated by combining all of the $\text{Im}(X_1)$ in some way; at the lowest concentrations, essentially by summing them. But the extra factor of $K(C_{d_1})$ in front of the bracket in Eq. 2, which is complex valued now, must also be taken into account.

Viscoelastic Materials in Silicone and Foamed Rubber Matrices

This group contains an example of a plastic material in silicone rubber, Fig. 27, in which the quadrupole dominates. The monopole and the dipole overlap each other.

When heavy inclusions are considered, the usual dipole predominance is conspicuous again (see Figs. 28 and 29). Note also that except for relaxation absorption, the host materials in Figs. 18 and 29 are identical.



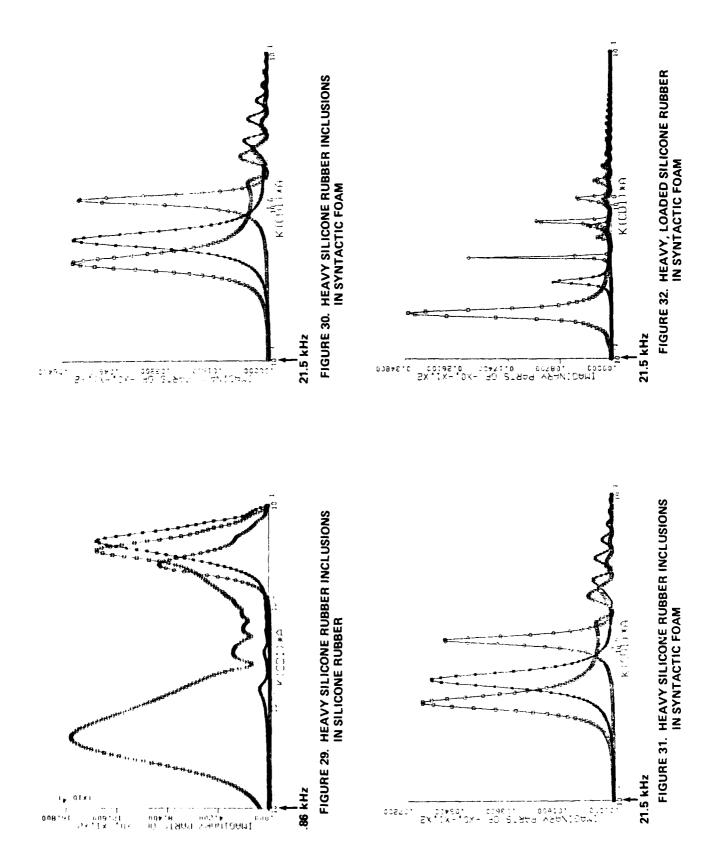


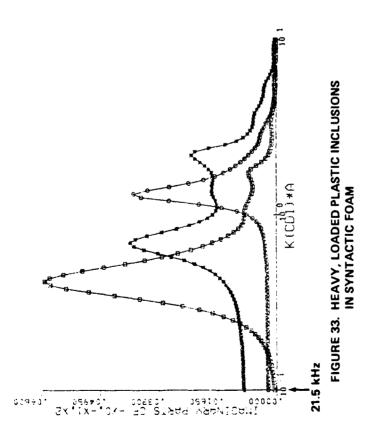
Viscoelastic Materials in Syntactic Foam

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As in the case of elastic foams, resonances are relatively sharp and the dipole is well isolated from the other two. Note also the multiplication factors we have used.

When the inclusions become more highly absorbing, the resonance peaks spread out but the dipole continues to dominate the spectrum (see Fig. 33).





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CHAPTER 5

CONCLUDING REMARKS

This brings us to the end of our survey. In Table 3 we have summarized the edge frequencies, f_Γ , of the materials in Tables 1 and 2 in monotonic order. Steel in very soft rubber gives the lowest and air in steel the highest $f_\Gamma.$ Between entries 9 and 10, air in rubber and heavy loaded silicone rubber in a heavy plastic there occurs almost a tripling of f_Γ , from 13.0 to 33.4 kHz. This is the dividing line between highly compressible fluids (air) or moderately heavy to heavy solid materials in relatively soft rubbery media on the one hand, where f_Γ is relatively low, and all other materials of this study, where f_Γ is relatively high.

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